

Paper 2014

For the next three (03) items that follow:

A straight line passes through $(1, -2, 3)$ and perpendicular to the plane $2x + 3y - z = 7$.

1. What are the direction ratios of normal to plane?
 - a. $\langle 2, 3, -1 \rangle$
 - b. $\langle 2, 3, 1 \rangle$
 - c. $\langle -1, 2, 3 \rangle$
 - d. None of the above
2. Where does the line meet the plane?
 - a. $(2, 3, -1)$
 - b. $(1, 2, 3)$
 - c. $(2, 1, 3)$
 - d. $(3, 1, 2)$
3. What is the image of the point $(1, -2, 3)$ in the plane?
 - a. $(2, -1, 5)$
 - b. $(-1, 2, -3)$
 - c. $(5, 4, 1)$
 - d. None of the above

For the next two (02) items that follow:

Consider the spheres $x^2 + y^2 + z^2 - 4y + 3 = 0$ and $x^2 + y^2 + z^2 + 2x + 4z - 4 = 0$.

4. What is the distance between the centres of the two spheres?
 - a. 5 unit
 - b. 4 unit
 - c. 3 unit
 - d. 2 unit
5. Consider the following statements:
 1. The two spheres intersect each other.
 2. The radius of first sphere is less than that of second sphere.
 Which of the above statements is/are correct?
 - a. 1 only
 - b. 2 only
 - c. Both 1 and 2
 - d. Neither 1 nor 2

For the next three (03) items that follow:

The vertices of a triangle ABC are $A(2, 3, 1)$, $B(-2, 2, 0)$ and $C(0, 1, -1)$.

6. What is the cosine of angle ABC?
 - a. $\frac{1}{\sqrt{3}}$
 - b. $\frac{1}{\sqrt{2}}$
 - c. $\frac{2}{\sqrt{6}}$
 - d. None of the above
7. What is the area of the triangle?
 - a. $6\sqrt{2}$ square unit
 - b. $3\sqrt{2}$ square unit
 - c. $10\sqrt{3}$ square unit
 - d. None of the above
8. What is the magnitude of the line joining mid points of the sides AC and BC?
 - a. $\frac{1}{\sqrt{2}}$ unit
 - b. 1 unit
 - c. $\frac{3}{\sqrt{2}}$ unit
 - d. 2 unit

For the next two (02) items that follow:

Consider the vectors $\vec{a} = \hat{i} - 2\hat{j} + \hat{k}$ and $\vec{b} = 4\hat{i} - 4\hat{j} + 7\hat{k}$.

9. What is the scalar projection of \vec{a} on \vec{b} ?
- a. 1 b. 19/9 c. 17/9 d. 23/9
10. What is the vector perpendicular to both the vectors?
- a. $-10\hat{i} - 3\hat{j} + 4\hat{k}$ b. $-10\hat{i} + 3\hat{j} + 4\hat{k}$
- c. $10\hat{i} - 3\hat{j} + 4\hat{k}$ d. None of the above

For the next two (02) items that follow:

Let a vector \vec{r} make angles 60° , 30° with x and y -axes respectively.

11. What angle does \vec{r} make with z -axis?
- a. 30° b. 60° c. 90° d. 120°
12. What are the direction cosines of \vec{r} ?
- a. $\left\langle \frac{1}{2}, \frac{\sqrt{3}}{2}, 0 \right\rangle$ b. $\left\langle \frac{1}{2}, -\frac{\sqrt{3}}{2}, 0 \right\rangle$
- c. $\left\langle \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0 \right\rangle$ d. $\left\langle -\frac{1}{2}, \frac{\sqrt{3}}{2}, 0 \right\rangle$

For the next two (02) items that follow:

Let $|\vec{a}| = 7$, $|\vec{b}| = 11$, $|\vec{a} + \vec{b}| = 10\sqrt{3}$

13. What is $|\vec{a} - \vec{b}|$ equal to?
- a. $2\sqrt{2}$ b. $2\sqrt{10}$ c. 5 d. 10
14. What is the angle between $(\vec{a} + \vec{b})$ and $(\vec{a} - \vec{b})$?
- a. $\frac{\pi}{2}$ b. $\frac{\pi}{3}$ c. $\frac{\pi}{6}$ d. None of the above
15. A line passes through the points $(6, -7, -1)$ and $(2, -3, 1)$. What are the direction ratios of the line?
- a. $\langle 4, -4, 2 \rangle$ b. $\langle 4, 4, 2 \rangle$
- c. $\langle -4, 4, 2 \rangle$ d. $\langle 2, 1, 1 \rangle$
16. From an aeroplane above a straight road the angles of depression of two positions at a distance 20 m apart on the road are observed to be 30° and 45° . The height of the aeroplane above the ground is:

- | | |
|---------------------|-----------------------|
| a. $10\sqrt{3}$ m | b. $10(\sqrt{3}-1)$ m |
| c. $10(\sqrt{3}+1)$ | d. 20 m |

17. Consider the following statements:

- There exists no triangle ABC for which $\sin A + \sin B = \sin C$.
- If the angles of a triangle are in the ratio 1:2:3, then its sides will be in the ratio $1:\sqrt{3}:2$.

Which of the above statements is/are correct?

- | | |
|-----------------|--------------------|
| a. 1 only | b. 2 only |
| c. Both 1 and 2 | d. Neither 1 nor 2 |

18. Consider the following statements:

- $\sin |x| + \cos |x|$ is always positive.
- $\sin(x^2) + \cos(x^2)$ is always positive.

Which of the above statements is/are correct?

- | | |
|-----------------|--------------------|
| a. 1 only | b. 2 only |
| c. Both 1 and 2 | d. Neither 1 nor 2 |

19. What is $\frac{1+\sin A}{1-\sin A} - \frac{1-\sin A}{1+\sin A}$ equal to?

- | | |
|---------------------------|---|
| a. $\sec A - \tan A$ | b. $2\sec A \cdot \tan A$ |
| c. $4\sec A \cdot \tan A$ | d. $4\operatorname{cosec} A \cdot \cot A$ |

20. What is $\frac{\cot 224^\circ - \cot 134^\circ}{\cot 226^\circ + \cot 316^\circ}$ equal to?

- | | |
|-------------------------------------|-------------------------------------|
| a. $-\operatorname{cosec} 88^\circ$ | b. $-\operatorname{cosec} 2^\circ$ |
| c. $-\operatorname{cosec} 44^\circ$ | d. $-\operatorname{cosec} 46^\circ$ |

21. Consider the following statements:

- $\tan^{-1} 1 + \tan^{-1}(0.5) = \pi/2$
- $\sin^{-1}(1/3) + \cos^{-1}(1/3) = \pi/2$

Which of the above statements is/are correct?

- | | |
|-----------------|--------------------|
| a. 1 only | b. 2 only |
| c. Both 1 and 2 | d. Neither 1 nor 2 |

22. If $A + B + C = \pi$, then what is $\cos(A+B) + \cos C$ equal to?

31. The cumulative frequency of the largest observed value must always be:
- Less than the total number of observations
 - Greater than the total number of observations
 - Equal to total number of observations
 - Equal to mid point of the last class interval
32. It has been found that if A and B play a game 12 times, A wins 6 times, B wins 4 times and they draw twice. A and B take part in a series of 3 games. The probability that they win alternately, is:
- a. $5/12$ b. $5/36$ c. $19/27$ d. $5/27$
33. Out of 7 consonants and 4 vowels, words are to be formed by involving 3 consonants and 2 vowels. The number of such words formed is:
- a. 25200 b. 22500 c. 10080 d. 5040
34. Let X denote the number of scores which exceed 4 in 18 tosses of a symmetrical die. Consider the following statements:
- The arithmetic mean of X is 6.
 - The standard deviation of X is 2.
- Which of the above statements is/are correct?
- a. 1 only b. 2 only
c. Both 1 and 2 d. Neither 1 nor 2
35. How many different words can be formed by taking four letters out of the letters of the word 'AGAIN' if each word has to start with A?
- a. 6 b. 12 c. 24 d. None of the above
36. The sum of the series formed by the sequence $3, \sqrt{3}, 1, \dots$ upto infinity is
- a. $\frac{3\sqrt{3}(\sqrt{3}+1)}{2}$ b. $\frac{3\sqrt{3}(\sqrt{3}-1)}{2}$
c. $\frac{3(\sqrt{3}+1)}{2}$ d. $\frac{3(\sqrt{3}-1)}{2}$
37. If $|z + \bar{z}| = |z - \bar{z}|$, then the locus of z is:
- A pair of straight lines
 - A line
 - A set of four straight lines
 - A circle
38. The number 251 in decimal system is expressed in binary system by:

- a. 11110111 b. 11111011 c. 11111101 d. 11111110

39. What is the argument of the complex number $\frac{(1+i)(2+i)}{3-i}$ where $i = \sqrt{-1}$?

- a. 0 b. $\frac{\pi}{4}$ c. $-\frac{\pi}{4}$ d. $\frac{\pi}{2}$

40. Consider the following statements in respect of the matrix $A = \begin{bmatrix} 0 & 1 & 2 \\ -1 & 0 & -3 \\ -2 & 3 & 0 \end{bmatrix}$:

1. The matrix A is skew-symmetric.
2. The matrix A is symmetric.
3. The matrix A is invertible.

Which of the above statements is/are correct?

- a. 1 only b. 3 only c. 1 and 3 d. 2 and 3

41. Consider two matrices $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \\ 1 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & -4 \\ 2 & 1 & -4 \end{bmatrix}$. Which one of the following is correct?

- a. B is the right inverse of A b. B is the left inverse of A
 c. B is the both sided inverse of A d. None of the above

42. One of the roots of $\begin{vmatrix} x+a & b & c \\ a & x+b & c \\ a & b & x+c \end{vmatrix} = 0$ is:

- a. abc b. $a+b+c$ c. $-(a+b+c)$ d. $-abc$

43. If A is any matrix, then the product AA is defined only when A is a matrix of order $m \times n$ where:

- a. $m > n$ b. $m < n$ c. $m = n$ d. $m \leq n$

44. The determinant of an odd order skew symmetric matrix is always:

- a. Zero b. One
 c. Negative d. Depends on the matrix

45. If any two adjacent rows or columns of a determinant are interchanged in position, the value of the determinant:

- a. Becomes zero b. Remains the same

53. What is $P(Z > 11)$ equal to?

- a. 0 b. $1/4$ c. $1/6$ d. $1/12$

54. What is $P(Z \text{ is the product of two prime numbers})$ equal to?

- a. 0 b. $1/2$ c. $1/4$ d. None of the above

For the next three (03) items that follow:

The number of telephone calls received in 245 successive one minute intervals at an exchange is given below in the following frequency distribution.

Number of calls	0	1	2	3	4	5	6	7
Frequency	14	21	25	43	51	40	39	12

55. What is the mean of the distribution?

- a. 3.76 b. 3.84 c. 3.96 d. 4.05

56. What is the median of the distribution?

- a. 3.5 b. 4 c. 4.5 d. 5

57. What is the mode of the distribution?

- a. 3 b. 4 c. 5 d. 6

For the next three (03) items that follow:

The mean and standard deviation of 100 items are 50, 5 and that of 150 items are 40, 6 respectively.

58. What is the combined mean of all 250 items?

- a. 43 b. 44 c. 45 d. 46

59. What is the combined standard deviation of all 250 items?

- a. 7.1 b. 7.3 c. 7.5 d. 7.7

60. What is the variance of all the 250 items?

- a. 50.6 b. 53.3 c. 55.6 d. 59.3

For the next three (03) items that follow:

In a survey of 25 students, it was found that 15 had taken Mathematics, 12 had taken Physics and 11 had taken Chemistry, 5 had taken Mathematics and Chemistry, 9 had taken Mathematics and Physics, 4 had taken Physics and Chemistry and 3 had taken all the three subjects.

61. The number of students who had taken only Physics is:

- a. 2 b. 3 c. 5 d. 6

62. The number of students who had taken only two subjects is:

- a. 7 b. 8 c. 9 d. 10

63. Consider the following statements:

1. The number of students who had taken only one subject is equal to the number of students who had taken only two subjects.
2. The number of students who had taken at least two subjects is four times the number of students who had taken all the three subjects.

Which of the above statements is/are correct?

- a. 1 only b. 2 only
c. Both 1 and 2 d. Neither 1 nor 2

For the next three (03) items that follow:

In the expansion of $\left(x^3 - \frac{1}{x^2}\right)^n$ where n is a positive integer, the sum of the coefficients of x^5 and x^{10} is 0.

64. What is n equal to?

- a. 5 b. 10 c. 15 d. None of the above

65. What is the value of the independent term?

- a. 5005 b. 7200 c. -5005 d. -7200

66. What is the sum of the coefficients of the two middle terms?

- a. 0 b. 1 c. -1 d. None of the above

For the next three (03) items that follow:

Given that $C(n, r) : C(n, r+1) = 1 : 2$ and $C(n, r+1) : C(n, r+2) = 2 : 3$.

67. What is n equal to?

- a. 11 b. 12 c. 13 d. 14

68. What is r equal to?

- a. 2 b. 3 c. 4 d. 5

69. What is $P(n, r) : C(n, r)$ equal to?

- a. 6 b. 24 c. 120 d. 720

70. The complete solution of $3\tan^2 x = 1$ is given by:

- a. $x = n\pi \pm \frac{\pi}{3}$ b. $x = n\pi + \frac{\pi}{3}$ only

c. $x = n\pi \pm \frac{\pi}{6}$

d. $x = n\pi + \frac{\pi}{6}$ only

71. What is the value of $\cos 36^\circ$?

a. $\frac{\sqrt{5}-1}{4}$

b. $\frac{\sqrt{5}+1}{4}$

c. $\frac{\sqrt{10+2\sqrt{5}}}{4}$

d. $\frac{\sqrt{10-2\sqrt{5}}}{4}$

72. Consider the following statements:

1. Value of $\sin \theta$ oscillates between -1 and 1 .

2. Value of $\cos \theta$ oscillates between 0 and 1 .

Which of the above statements is/are correct?

a. 1 only

b. 2 only

c. Both 1 and 2

d. Neither 1 nor 2

73. If x and y are positive and $xy > 1$, then what is $\tan^{-1} x + \tan^{-1} y$ equal to?

a. $\tan^{-1} \left(\frac{x+y}{1-xy} \right)$

b. $\pi + \tan^{-1} \left(\frac{x+y}{1-xy} \right)$

c. $\pi - \tan^{-1} \left(\frac{x+y}{1-xy} \right)$

d. $\tan^{-1} \left(\frac{x-y}{1+xy} \right)$

74. Consider the following statements:

1. $n \left(\sin^2 67\frac{1}{2}^\circ - \sin^2 22\frac{1}{2}^\circ \right) > 1$ for all positive integers $n \geq 2$.

2. If x is any positive real number, then $nx > 1$ for all positive integers $n \geq 2$.

Which of the above statements is/are correct?

a. 1 only

b. 2 only

c. Both 1 and 2

d. Neither 1 nor 2

75. Consider the following statements:

1. If 3θ is an acute angle such that $\sin 3\theta = \cos 2\theta$, then the measurement of θ in radians equals to $\frac{\pi}{10}$.

2. One radian is the angle subtended at the centre of a circle by an arc of the same circle whose length is equal to the diameter of that circle.

Which of the above statements is/are correct?

a. 1 only

b. 2 only

82. What is the maximum value of the function?
 a. $1/2$ b. $1/3$ c. 2 d. 3
83. What is the minimum value of the function?
 a. $1/2$ b. $1/3$ c. 2 d. 3

For the next three (03) items that follow:

Let $f(x)$ be a function defined in $1 \leq x < \infty$ by

$$f(x) = \begin{cases} 2-x & \text{for } 1 \leq x \leq 2 \\ 3x-x^2 & \text{for } x > 2 \end{cases}$$

84. Consider the following statements:
- The function is continuous at every point in the interval $[1, \infty)$.
 - The function is differentiable at $x = 1.5$.
- Which of the above statements is/are correct?
- a. 1 only b. 2 only
 c. Both 1 and 2 d. Neither 1 nor 2
85. What is the differentiable coefficient of $f(x)$ at $x = 3$?
 a. 1 b. 2 c. -1 d. -3

86. Consider the following statements:
- $f'(2+0)$ does not exist.
 - $f'(2-0)$ does not exist.
- Which of the above statements is/are correct?
- a. 1 only b. 2 only
 c. Both 1 and 2 d. Neither 1 nor 2

87. What is $\int_0^{\frac{\pi}{2}} \ln(\tan x) dx$ equal to?
 a. $\ln 2$ b. $-\ln 2$ c. 0 d. None of the above

For the next three (03) items that follow:

The general solution of the differential equation $(x^2 + x + 1)dy + (y^2 + y + 1)dx = 0$ is $(x + y + 1) = A(1 + Bx + Cy + Dxy)$ where B , C and D are constant and A is parameter.

88. What is B equal to?
 a. -1 b. 1 c. 2 d. None of the above

89. What is C equal to?
 a. 1 b. -1 c. 2 d. None of the above
90. What is D equal to?
 a. -1 b. 1 c. -2 d. None of the above
91. What is $\lim_{x \rightarrow 0} \frac{(1+x)^n - 1}{x}$ equal to?
 a. 0 b. 1 c. n d. $n - 1$
92. What is $\lim_{x \rightarrow 0} \frac{x}{\sqrt{1 - \cos x}}$ equal to?
 a. $\sqrt{2}$ b. $-\sqrt{2}$ c. $\frac{1}{\sqrt{2}}$ d. Limit does not exist
93. What is the derivative of $\sqrt{\frac{1 + \cos x}{1 - \cos x}}$?
 a. $\frac{1}{2} \sec^2 \frac{x}{2}$ b. $-\frac{1}{2} \operatorname{cosec}^2 \frac{x}{2}$
 c. $-\operatorname{cosec}^2 \frac{x}{2}$ d. None of these
94. What is $\int_0^1 \frac{e^{\tan^{-1} x} dx}{1+x^2}$ equal to?
 a. $e^{\frac{\pi}{4}} - 1$ b. $e^{\frac{\pi}{4}} + 1$ c. $e - 1$ d. e
95. What is the slope of the tangent to the curve $y = \sin^{-1}(\sin^2 x)$ at $x = 0$?
 a. 0 b. 1 c. 2 d. None of the above
96. The solution of $\frac{dy}{dx} = |x|$ is:
 a. $y = \frac{x|x|}{2} + c$ b. $y = \frac{|x|}{2} + c$
 c. $y = \frac{x^2}{2} + c$ d. $y = \frac{x^3}{2} + c$
- where c is an arbitrary constant
97. What is the solution of $\frac{dy}{dx} + 2y = 1$ satisfying $y(0) = 0$?

a. $y = \frac{1 - e^{-2x}}{2}$

b. $y = \frac{1 + e^{-2x}}{2}$

c. $y = 1 + e^x$

d. $y = \frac{1 + e^x}{2}$

For the next two (02) items that follow:

Consider the curve $y = e^{2x}$.

98. What is the slope of the tangent to the curve at (0, 1)?

- a. 0 b. 1 c. 2 d. 4

99. Where does the tangent to the curve at (0, 1) meet the x -axis?

- a. (1, 0) b. (2, 0) c. (-1/2, 0) d. (1/2, 0)

For the next two (02) items that follow:

Consider an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.

100. What is the area of the greatest rectangle that can be inscribed in the ellipse?

- a. ab b. $2ab$ c. $ab/2$ d. \sqrt{ab}

101. What is the area included between the ellipse and the greatest rectangle inscribed in the ellipse?

- a. $ab(\pi - 1)$ b. $2ab(\pi - 1)$
c. $ab(\pi - 2)$ d. None of the above

For the next two (02) items that follow:

Consider the integrals

$$I_1 = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{dx}{1 + \sqrt{\tan x}} \quad \text{and} \quad I_2 = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sqrt{\sin x} dx}{\sqrt{\sin x} + \sqrt{\cos x}}$$

102. What is $I_1 - I_2$ equal to?

- a. 0 b. $2I_1$ c. π d. None of the above

103. What is I_1 equal to?

- a. $\pi/24$ b. $\pi/18$ c. $\pi/12$ d. $\pi/6$

For the next two (02) items that follow:

Consider the function $f(x) = \frac{1 - \sin x}{(\pi - 2x)^2}$ where $x \neq \frac{\pi}{2}$ and $f\left(\frac{\pi}{2}\right) = \lambda$

104. What is $\lim_{x \rightarrow \frac{\pi}{2}} f(x)$ equal to?
- a. 1 b. 1/2 c. 1/4 d. 1/8
105. What is the value of λ if the function is continuous at $x = \frac{\pi}{2}$?
- a. 1/8 b. 1/4 c. 1/2 d. 1
106. Let X be the set of all citizens of India. Elements x, y in X are said to be related if the difference of their age is 5 years. Which one of the following is correct?
- a. The relation is an equivalence relation on X .
- b. The relation is symmetric but neither reflexive nor transitive.
- c. The relation is reflexive but neither symmetric nor transitive.
- d. None of the above
107. Consider the following relations from A to B where $A = \{u, v, w, x, y, z\}$ and $B = \{p, q, r, s\}$.
- $\{(u, p), (v, p), (w, p), (x, q), (y, q), (z, q)\}$
 - $\{(u, p), (v, q), (w, r), (z, s)\}$
 - $\{(u, s), (v, r), (w, q), (u, p), (v, q), (z, q)\}$
 - $\{(u, q), (v, p), (w, s), (x, r), (y, q), (z, s)\}$
- Which of the above relations are not functions?
- a. 1 and 2 b. 1 and 4 c. 2 and 3 d. 3 and 4
108. If α and β are the roots of the equation $ax^2 + bx + c = 0$, where $a \neq 0$, then $(a\alpha + b)(a\beta + b)$ is equal to:
- a. ab b. bc c. ca d. abc
109. Let S denote set of all integers. Define a relation R on S as ' aRb if $ab \geq 0$ where $a, b \in S$ '. Then R is:
- a. Reflexive but neither symmetric nor transitive relation
- b. Reflexive, symmetric but not transitive relation
- c. An equivalence relation
- d. Symmetric but neither reflexive nor transitive relation
110. The roots of the equation $2a^2x^2 - 2abx + b^2 = 0$ when $a < 0$ and $b > 0$ are:
- a. Sometimes complex b. Always irrational
- c. Always complex d. Always real

111. What is the sum of the two numbers $(11110)_2$ and $(1010)_2$?
- a. $(101000)_2$ b. $(110000)_2$
c. $(100100)_2$ d. $(101100)_2$
112. Let N denote the set of all non-negative integers and Z denote the set of all integers. The function $f : Z \rightarrow N$ given by $f(x) = |x|$ is:
- a. One-one but not onto b. Onto but not one-one
c. Both one-one and onto d. Neither one-one nor onto
113. If P and Q are two complex numbers, then the modulus of the quotient of P and Q is:
- a. Greater than the quotient of their moduli
b. Less than quotient of their moduli
c. Less than or equal to the quotient of their moduli
d. Equal to the quotient of their moduli
114. Let $z = x + iy$ where x, y are real variables and $i = \sqrt{-1}$. If $|2z - 1| = |z - 2|$, then the point z describes:
- a. A circle b. An ellipse
c. A hyperbola d. A parabola
115. The sum of an infinite GP is x and the common ratio r is such that $|r| < 1$. If the first term of the GP is 2, then which one of the following is correct?
- a. $-1 < x < 1$ b. $-\infty < x < 1$
c. $1 < x < \infty$ d. None of the above
116. A box contains 3 white and 2 black balls. Two balls are drawn at random one after the other. If the balls are not replaced, what is the probability that both the balls are black?
- a. $2/5$ b. $1/5$ c. $1/10$ d. None of the above
117. For two variables x and y , the two regression coefficients are $b_{yx} = -3/2$ and $b_{xy} = -1/6$. The correlation coefficient between x and y is:
- a. $-1/4$ b. $1/4$ c. $-1/2$ d. $1/2$
118. The variance of numbers $x_1, x_2, x_3, \dots, x_n$ is V . Consider the following statements:
1. If every x_i is increased by 2, the variance of the new set of numbers is V .
2. If the numbers x_i is squared, the variance of the new set is V^2 .
- Which of the following statements is/are correct?
- a. 1 only b. 2 only

